

Semiconductors

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Intrinsic semiconductor $\rightarrow$

Semiconductor without any impurities

Ex. Si, Ge, $\rightarrow$ Pure Crystals.

forbidden gap $\approx 1 \text{ eV}$.

there are two possibilities for transition of e^- from valence band to Conduction band.

- $\rightarrow$ Applying Electric field
- $\rightarrow$ thermal excitation.

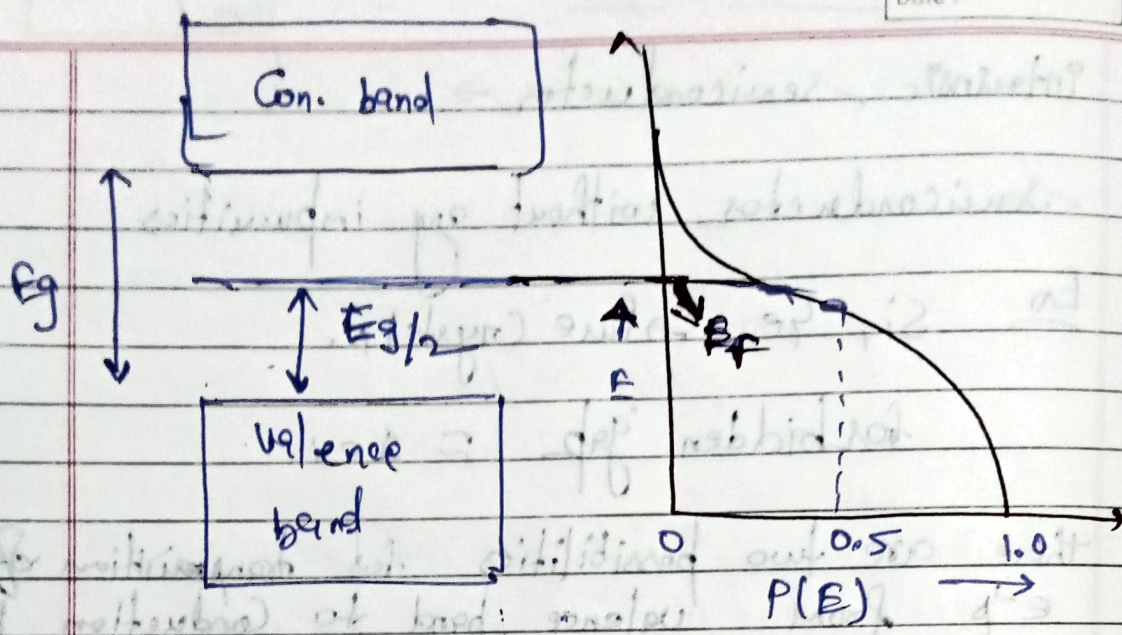
At room temp., the thermal energy that is available can excite a limited no. of electrons across the energy gap.

this limited no. of e^- accounts for semi-conduction.

no. of e^- excited given by fermi-Dirac probability distribution $\rightarrow$

$$f_d = P(E) = \frac{1}{1 + e^{(E-E_F)/KT}}$$

E_F lies midway in forbidden gap for semiconductors.



Now we can conclude that

$$E - E_f = E_g/2$$

therefore

$$P(E) = \exp\left[\frac{-E_g}{2KT}\right]$$

Probability
of finding
 e^-
let.

{ 1 can be neglected
as it is very v. small
in comparison to $\exp$

$$P(E) = n$$

then

$$n = N \exp\left[\frac{-E_g}{2KT}\right]$$

↑
no. of e^-
available for
excitation.

The promotion of some of e^- across the gap leaves some vacant e^- sites in valence band. these are called holes.

$$N_e = N_h$$

$$\text{Mobility} = \frac{\text{drift velocity}}{\text{field gradient}}$$

$$\left. \begin{aligned} J_e &= -n_e e \mu_e E \\ J_h &= n_h e \mu_h E \end{aligned} \right\} \rightarrow J = \sigma \vec{E}$$

$$J_e = + n_e e \mu_e E \rightarrow \text{dir of flow of } e^- \text{ opposite to electric field.}$$

$$J_h = n_h e \mu_h E \rightarrow \text{dir of hole (+ve charge) same as electric field.}$$

$$\Rightarrow J = J_e + J_h$$

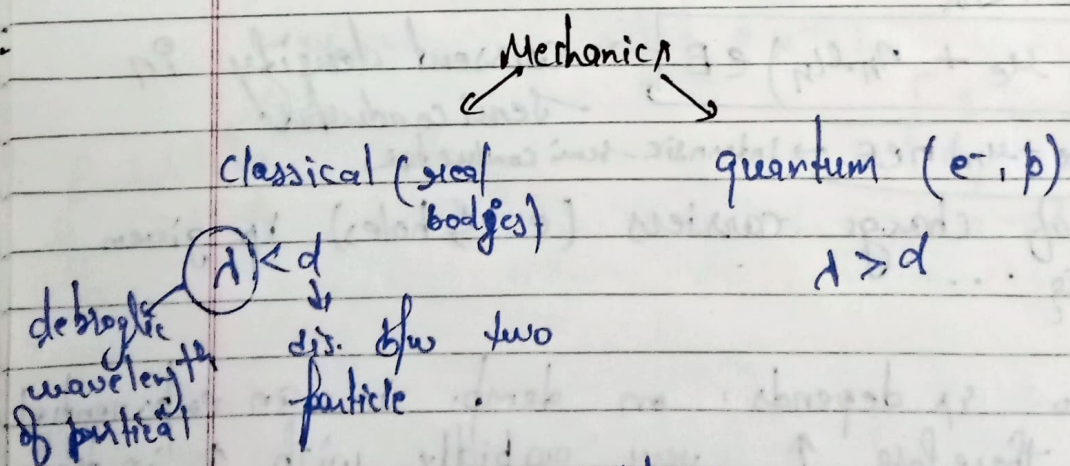
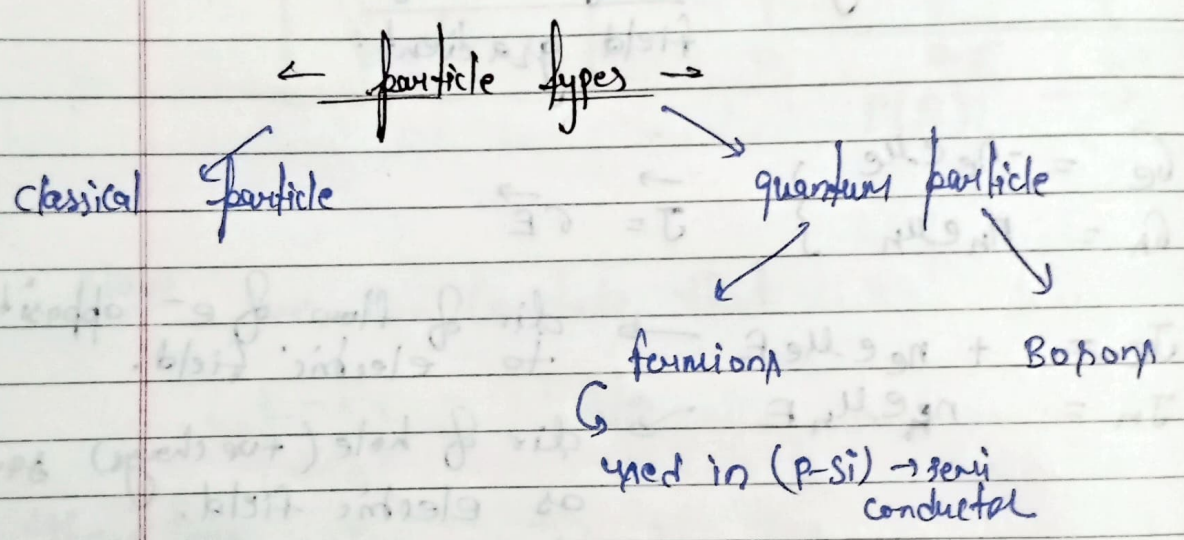
$$J = (n_e \mu_e + n_h \mu_h) e E \rightarrow \text{current density in semiconductor}$$

$$[n_e = n_h] \quad J = (\mu_e + \mu_h) n_e E \rightarrow \text{intrinsic semiconductor}$$

- No. of charge carriers (e^- & holes) is given the eq.
- This no. is depends on temp. in an exponential way, therefore $\uparrow$ very rapidly with $\uparrow$ in temp.
- Conduction also $\uparrow$ in some manners.
- plot of logarithm of conductivity against the reciprocal of temp. yields straight line.
- slope of this st. line give energy gap

to make free e^- we require 0.025 eV energy
and at room temp. we have thermal energy (kT)
 $= 0.026 \text{ eV}$.

thus we always have enough energy :

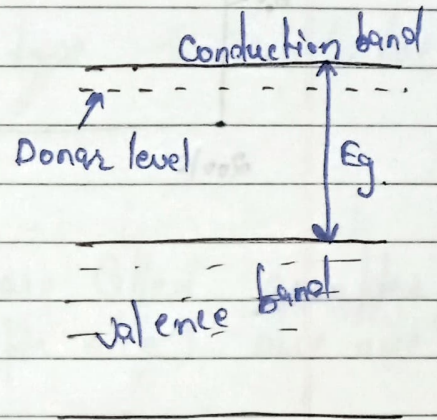
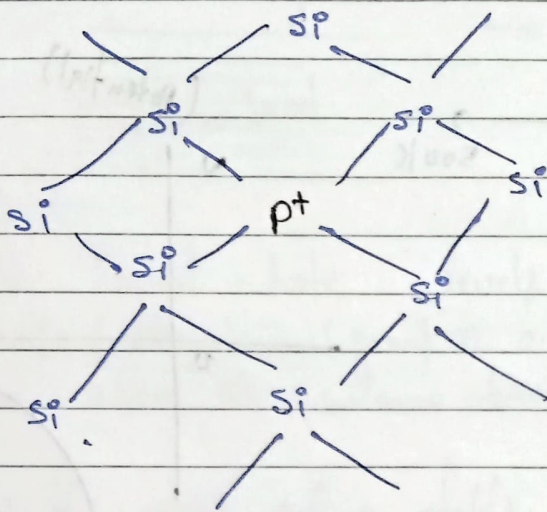


de Broglie wavelength $(\lambda) = \frac{h}{p}$ $p \rightarrow$ momentum

distribution function $\rightarrow$

$f_{FD}(E) = \frac{1}{1 + e^{(E - E_F)/kT}}$ $\rightarrow$ finding of particles at temp. T .

Extrinsic Semiconductor $\rightarrow$ the conduction is due to the presence of extraneous impurities.



$$n_e \neq n_h$$

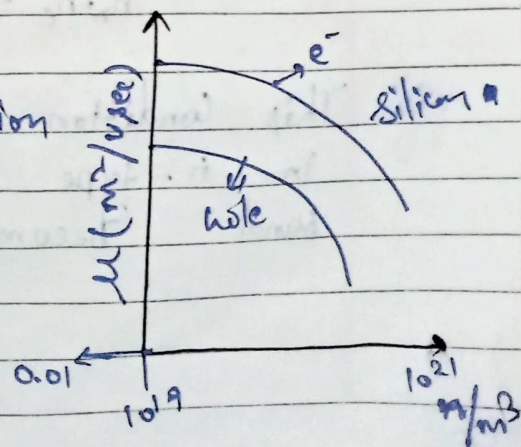
$$J = (n_e \mu_e + n_h \mu_h) e E$$

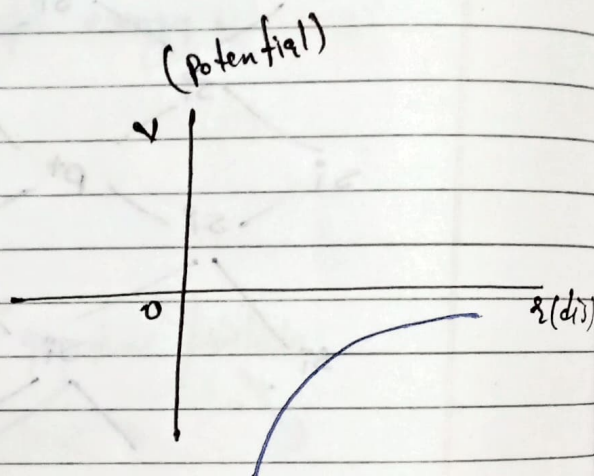
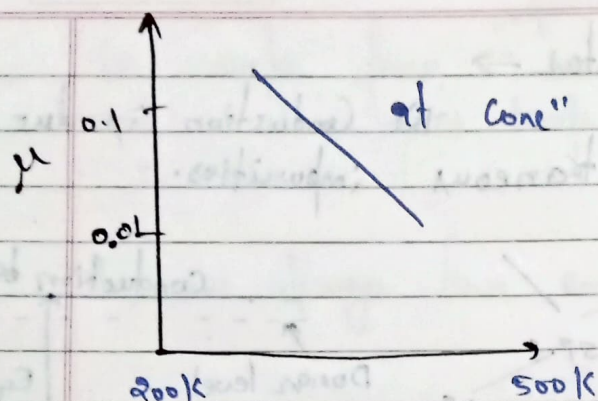
if $n_e > n_h \rightarrow$ n type
due to pentavalent
 $n_h > n_e \rightarrow$ P type
due to divalent
impurity

$$\mu_H \propto \frac{T^{3/2}}{N_I} \quad \& \quad \mu_e \propto T^{-3/2}$$

mobility depends upon $\rightarrow$

- (i) impurity concentration
- (ii) temperature.



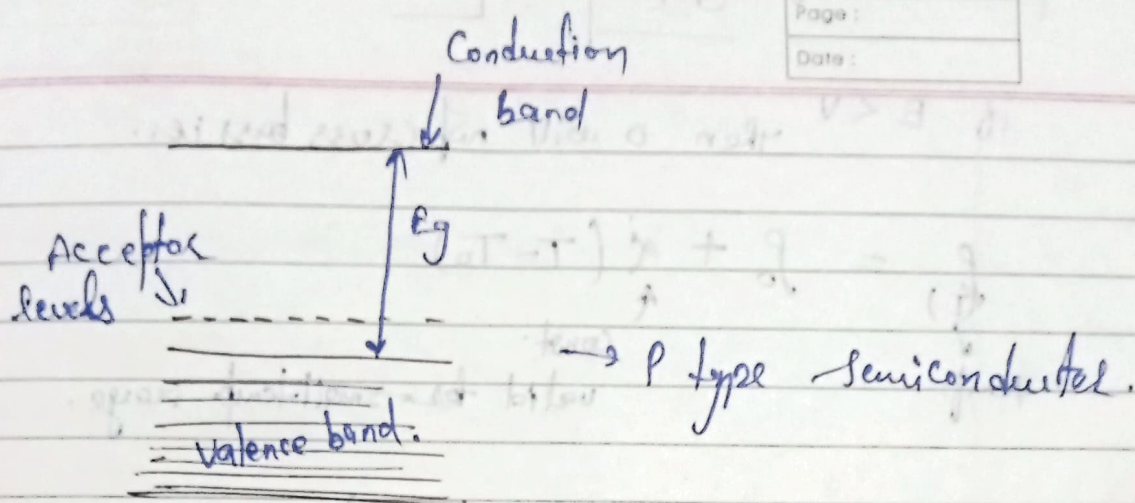


- Silicon atom in diamond cubic structure. four of five electrons in the outermost orbital of the phosphorus atom take part in the tetrahedral bonding with the four silicon bonding.

Acc. to law of mass action, the product of no. of e^{-} in the conduction band and the no. of holes in the valence band must be constant.
i.e.

$$n \cdot n_e = \text{constant}$$

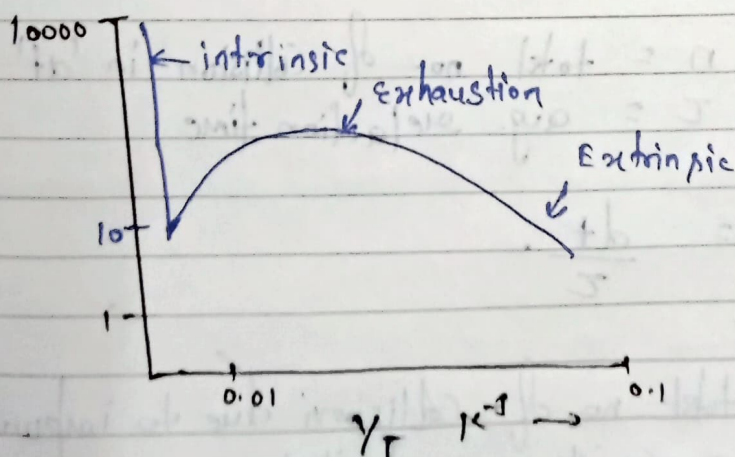
This condition drastically reduces the no. of hole in n -type semiconductor. e^{-} in conduction band become the majority charge carriers.



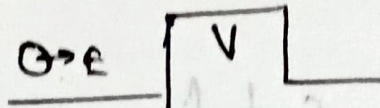
The bound-hole levels are called acceptor levels (Aluminium (group 13) accepts an e^-) are just above the valence band.

- law of mass action holds good here also.

A typical plot of the logarithm of conductivity against temp.



from the slope of st. lines ionization energy of the impurities can be calculated.



If $E < V$ then ϕ will not cross barrier.

$$\rho(T) = \rho_0 + \alpha (T - T_0)$$

$\uparrow$ temp $\uparrow$ const. $\downarrow$ valid for small-temp range.

due to impurity / lattice vibration

additive nature of resistivity →

$$\rho = \rho_I + \rho_L + \rho_0$$

$$\rho = \frac{1}{\sigma} = \frac{1}{n e v_d} = \frac{E}{n e v_d}$$

Resistance → due to scattering of charge carriers

let n = total no. of collision in 'dt' time:
 τ = avg. relaxation time

$$n = \frac{dt}{\tau}$$

n_I = total no. of collision due to impurity in time
 τ_I = avg time (impurity)

$$n_I = \frac{dt}{\tau_I}$$

similarly n_L & τ_L for lattice

$$n_L = \frac{dt}{\tau_L}$$

$$n = n_i + n_e$$

$$\frac{dn}{dt} = \frac{dn_i}{dt} + \frac{dn_e}{dt} = \frac{1}{\tau} = \frac{1}{\tau_i} + \frac{1}{\tau_e}$$

Extra, other than this class.

force on e^-

$$F = -eE = m_e^* \frac{dv}{dt}$$

$$\int_0^v dv = \int_0^T \frac{-eEt}{m_e^*}$$

$\Rightarrow$

$$v = \frac{-eEt}{m_e^*}$$

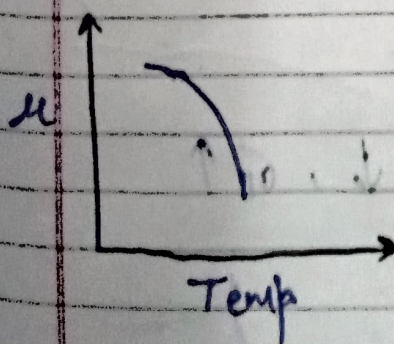
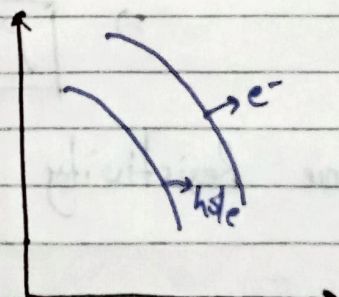
$$v_d = \frac{-eEt}{m_e^*}$$

drift velocity

$$\mu_i \propto \frac{T^{3/2}}{N_i}$$

$$\& \mu_e \propto T^{-3/2}$$

μ
↑
overall



$$\frac{1}{\tau} = \frac{1}{\tau_i} + \frac{1}{\tau_e}$$

avg. scab time

$$\frac{1}{\tau} = \frac{1}{\tau_I} + \frac{1}{\tau_L}$$

$$\frac{1}{\mu \frac{M^*}{e}} = \frac{1}{\mu_I \left(\frac{M^*}{e} \right)} + \frac{1}{\mu_L \left(\frac{M^*}{e} \right)}$$

$$\Rightarrow \frac{1}{\mu} = \frac{1}{\mu_I} + \frac{1}{\mu_L}$$

$$\mu = \frac{\mu_I \mu_L}{\mu_I + \mu_L}$$

$$\frac{1}{n \mu_e} = \frac{1}{n_I \mu_e} + \frac{1}{n_L \mu_e}$$

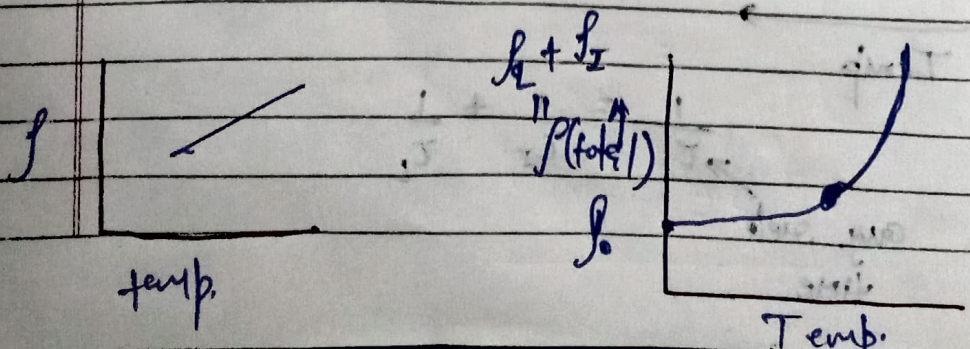
$$\Rightarrow \frac{1}{\sigma} = \frac{1}{\sigma_I} + \frac{1}{\sigma_L} \quad \left(\because \sigma = n e \mu \right)$$

$$\Rightarrow \rho = \rho_I + \rho_L$$

Resistivity is additive in nature.

$$\rho_L = \frac{1}{n e \mu_L} \propto \mu_L \propto \frac{1}{T^{3/2}}$$

as temp. $\downarrow$ $\mu_L \uparrow$ & $\rho_L \downarrow$, $\sigma_L \uparrow$



$$\mu_H = \frac{\tau^{3/2}}{N_I}$$

if remain almost const.
at all temp. or
have a minor change
can be neglected.

* velocity of e^- in material (v)

$$= \sqrt{\frac{3kT}{m_e}}$$

$$f = ma$$

$$-eE = m a$$

$$a = \frac{-eE}{m}$$

bec. when we
apply electric field

u = initial velocity of e^-
 v = velocity of e^-

$$v = u + at$$

$$u + \left(\frac{-eE}{m}\right)t$$

$$\langle v \rangle = \langle u \rangle + \left(\frac{-eE}{m}\right)\langle t \rangle$$

v_d

$$\Rightarrow v_d = \left(\frac{-eE}{m_e^*}\right)\tau$$

ohm's law $\rightarrow$

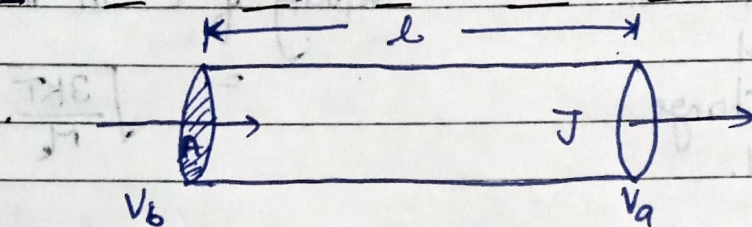
$$J = \sigma E \quad (1)$$

$$= -ne\mu E = -nev_d$$

$$J = -ne \left(\frac{-eE}{m_e^*}\right)\tau = \frac{ne^2 E \tau}{m_e^*}$$

$$\Rightarrow J = \left(\frac{ne^2 \tau}{m_e^*}\right) E \quad (ii)$$

$$\sigma = \frac{ne^2\tau}{m_e} \rightarrow \text{drude Model.}$$



$$\Delta V = V_b - V_a = \int_a^b E \cdot dl = E(l)$$

$$\Rightarrow E = \frac{\Delta V}{l}$$

$$J = \sigma E$$

$$J = \frac{\sigma \Delta V}{l} \Rightarrow \Delta V = \frac{Jl}{\sigma} = \frac{I}{A} \cdot \frac{l}{\sigma} = I \left(\frac{\rho l}{A} \right)$$

$$\Rightarrow \Delta V = IR$$

Conductivity

or

$$J = \sigma E \Rightarrow J \propto E$$

at microscopic

$$\text{When } \sigma = \frac{ne^2\tau}{m_e}$$

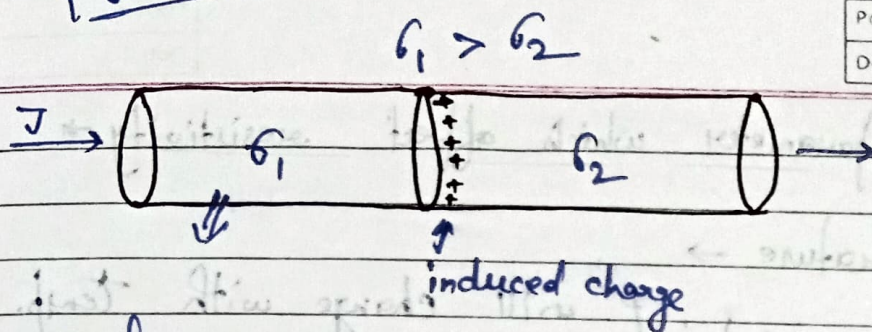
$$\frac{I}{A} = \sigma \frac{\Delta V}{l} \Rightarrow \Delta V = \left(\frac{\rho l}{A} \right) I$$

$$\Delta V = IR$$

$$J = \sigma E$$

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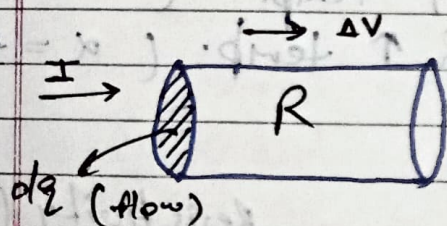
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will have more
no. of charge carriers.
i.e. e^-

$$J = \sigma_2 E_2 = \sigma_1 E_1$$

$$\Rightarrow E_2 = \frac{\sigma_1 E_1}{\sigma_2}$$



Energy

$$dU = dq \cdot \Delta V$$

$$P = \frac{dU}{dt} = \left(\frac{dq}{dt} \right) \cdot \Delta V = I \cdot \Delta V$$

$$I \cdot R$$

$$P = I \cdot I \cdot R$$

$$P = I^2 R$$

** Some values.

$$\sigma_{Cu} = 5.81 \times 10^7 \text{ S/m}$$

$$\sigma_{Al} = 3.55 \times 10^7 \text{ S/m}$$

The parameter which affect resistivity →

(i) Temperature →

ρ will change with temp. acc. to given relation.

$$\rho(T) = \rho(T_0) [1 + \alpha (T - T_0)]$$

for metals → $\rho \uparrow$ with $\uparrow$ temp. ($\alpha = +ve$)

for semiconductor → $\rho \downarrow$ with $\uparrow$ temp. ($\alpha = +ve$)

Metals	Temp. Coeff. ($1/^\circ C$)	Resistivity (Ωm)
Silver	0.0061	159×10^{-8}
Copper	0.0068	1.68×10^{-8}
Gold	0.0034	2.44×10^{-8}
Aluminium	0.00429	2.65×10^{-8}
Graphite	-0.0005	
Germanium	-0.05	
Si	-0.07	

$\rho \uparrow$ very fastly.

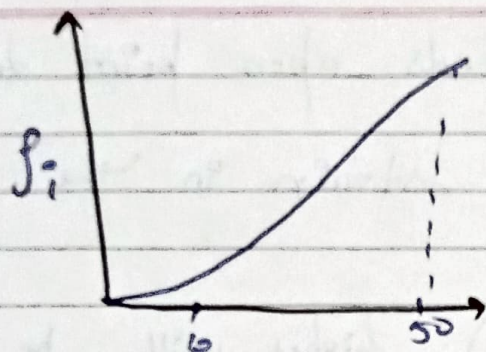
(ii) Alloying →

Alloy → Solid solution

$$\rho_i = A(1 - C_i)C_i$$

$C_i \rightarrow$ % concⁿ of impurity added.
(Cu-Ni)

$A = \text{const.}$



(iii) Volume fraction →

$$\rho = \rho_A V_A + \rho_B V_B$$

↑
Volume fraction

A & B are two phases of same metal. (e.g., Fe^{14}Fe)
non metal.

$$E_n = \left(n + \frac{1}{2}\right) \hbar \omega \leftarrow \text{discrete energy}$$

$$p = \hbar \omega = \frac{\hbar}{2\pi} \cdot \frac{2\pi}{\lambda} \Rightarrow p = \frac{\hbar}{\lambda}, \quad E = \frac{p^2}{2m}$$

$$\Rightarrow \boxed{E = \frac{\hbar^2 k^2}{2m}}$$

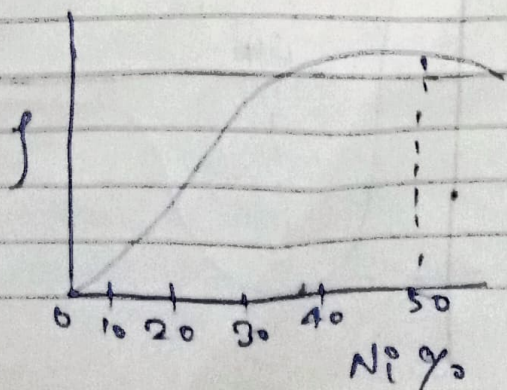
factor affecting Resistivity

impurity

(iv) impurities →

Ni, In Cu

on adding impurities in metal it ↑ ρ.



Q1) Stress $\rightarrow$ (μ depends upon point defect)
 ($\downarrow$ gives rise to strain in the lattice)

More (higher strain) higher will be resistivity
 (due to twisting a metal piece)

to solve this problem

Annealing process $\rightarrow$

used for

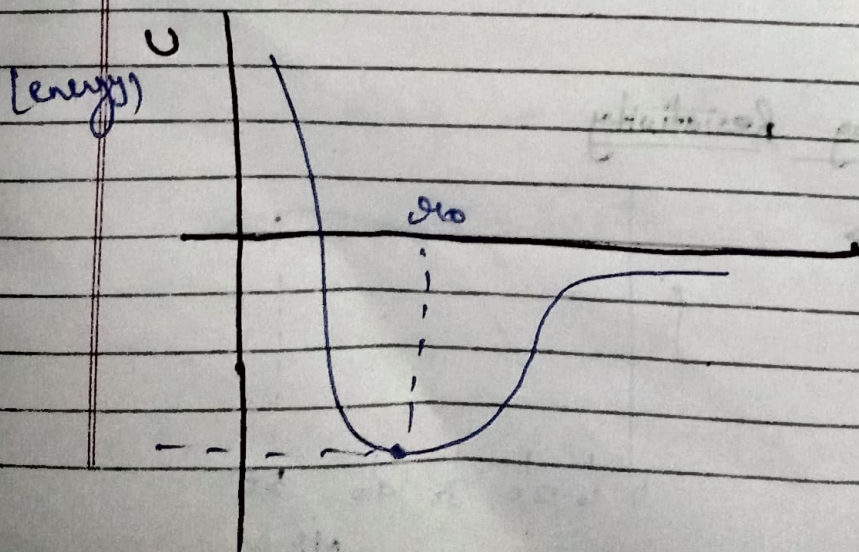
to remove local strain

ρ will decrease as strain is removed

Twisted
 $\rightarrow$ heat metal at higher temp. below melting temp. and then cool it at room temp.

(Note Resistivity will be noted at room temp.)

Atom will such that they have lowest energy



cvi

Age hardening →

after adding small amount of impurity and heating for a long time at lower temp than its melting point.

Strength will be more than pure solid.

- 1st add impurity.
- heat at higher temp.
- get a solid solⁿ
- then cool down.

f ↑ as impurities ↑

NOTE → In alloys impurities may not be homogeneous but here it is.

29/06/23

Set 02

$$\rho = \rho_p + \rho_I + \rho_d \rightarrow \text{deformation}$$

↓ ↓
phonos impurities

(S.No Metals symbol Resistivity ($\mu\Omega\text{-cm}$) Temp. Coeff. ($1/^\circ\text{C}$) Thermal Conductivity)

$$\rho = \rho_0 [1 + \alpha(T - T_0)]$$

S.No.	Metals	symbol	Resistivity ($\mu\Omega\text{-cm}$)	temp. Coeff. ($1/^\circ\text{C}$)	Thermal conductivity (W/mK)	density (g/cm^3)	m.p ($^\circ\text{C}$)
1.	*Silver	Ag	1.58	0.0038	429	10.49	962
2.	Copper	Cu	1.68	0.00386	385	8.96	1085
3.	Gold	Au	2.21	0.0034	310	19.3	1064
4.	Aluminium	Al	2.65	0.00429	205	2.7	660

making (vap. deposition).
not used because it is poisonous

Generally, ~~Cu~~ can not be soldering.

Thermal Expansion Coefficient ($1/^\circ\text{C}$)

Cu $\leftarrow$ 0.0000167
Al $\leftarrow$ 0.00429

used in RND (Research field)
bare gold film

sinter on

Quiz -2
on 7th June

~~30/05/23 செல்~~



 used for
 power (electricity)
 transportations.

- Al $\rightarrow$ ~~used~~ also used in Aircraft. (due to light weight)
- Cu ^(wire) $\rightarrow$ used in housing item.
- to $\uparrow$ strength of wire, impurities are added.
- alloy (Al + Cu) so that No Corrosion and fissures.
- strain over head wire (Cd in Cu)
 - $\downarrow$ in very low %
 - (0.8 to 1)%
- Silver - Tungsten (good for mech. strength and Co-operations)

Good Conductors

Ag, Cu, Au, Al $\rightarrow$ making wires.